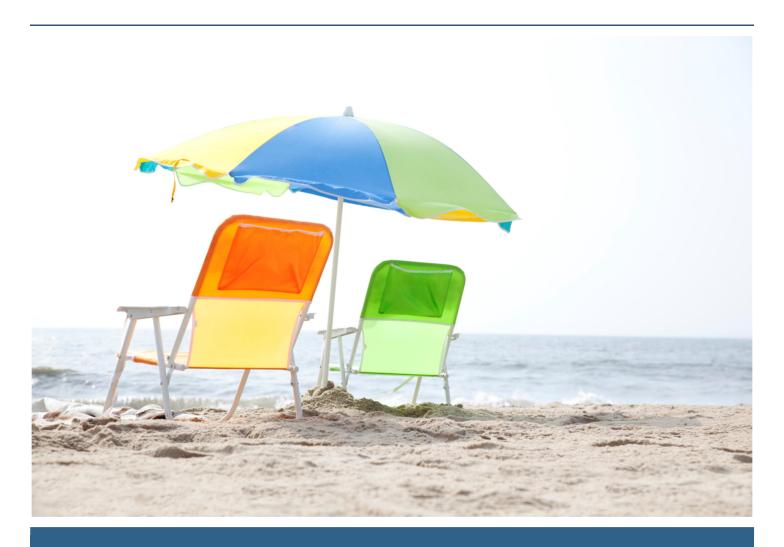
# ST. GREGORY THE GREAT CATHOLIC SCHOOL SUMMER 2024 READING AND MATH ENRICHMENT



# Students Entering Eighth Grade August 2024

Dear St. Gregory Parents,

Happy summer! While you are enjoying your summer, please encourage your child to read as much as possible. Reading is one of the most important skills which can impact your child's academic success and confidence!

The following pages have information regarding the math and reading activities our eighth teachers would like your child to complete during the summer. Please send the completed activities with your child on the second day of school.

# Incoming 8<sup>th</sup> Grade Summer Reading

Incoming 8<sup>th</sup> graders are required to read one *ONE* novel and are encouraged to read more.

Mandatory: An Elephant in the Garden by Michael Morpurgo

ISBN: 978-1250034144



Please complete the story reflection for An Elephant in the Garden and turn in on the second day of school. Students will take an AR test on An Elephant in the Garden upon returning to school. Students do not have to take an AR test on the other novels read. Please note that NO AR quizzes will be deleted. Please be prepared and plan accordingly.

An Elephant in the Garden Novel Reflection. You may write (in cursive and blue ink) or type your responses on a google document.

- 1. Who was your favorite main character in this story? What are the actions and personality traits of the character that you found to be most likable or appealing?
- 2. What is the author's purpose for the story? Use text evidence to support your claim?
- 3. What is a theme (idea or message) embedded within the story that stands out to you? Quote a passage from the book that sticks to memory, and explain why that idea or message impressed you so much.
- 4. What is the greatest conflict or hardship experienced by your favorite main character? How did their hardship affect your emotions while reading the novel? Did you feel anxiousness, sadness, compassion or empathy for the character? Describe the emotion you experienced during this point of the story and explain why you felt this way.
- 5. Summarize the climax of the story. How does the climax affect your favorite main character? Does the climax create greater happiness for them? Does it allow him to accomplish his goal(s) within the story? Please explain.
- 6. If you were your favorite character, what would you have done differently to avoid encountering his/her problem? Think about a decision that this character made at some point in the story which you did not quite agree with. How would you have made this decision differently? Explain why.

I read An Elephant in the Garden and will be taking the AR	quiz on An Elephant in the Garden upon returning to school

# Operations with Integers

## Adding Integers

 <u>Negative + Negative</u>: Add the absolute values of the two numbers and make the answer negative.

ex: 
$$-5 + (-9)$$
  $\longrightarrow$   $5 + 9 = 14$   $\longrightarrow$  answer:  $(-14)$ 

 <u>Negative + Positive (or Positive + Negative)</u>: Subtract the absolute values of the two numbers (larger minus smaller) and take the sign of the number with the greater absolute value.

ex: 
$$-7 + 12 \longrightarrow 12 - 7 = 5 \longrightarrow 12 > 7$$
, so answer is positive  $\longrightarrow$  answer:  $5$ 

ex: 
$$6 + (-9)$$
  $\longrightarrow$   $9 - 6 = 3$   $\longrightarrow$   $9 > 6$ , so answer is negative  $\longrightarrow$  answer:  $(-3)$ 

### Subtracting Integers

• Keep the first number the same, change the subtraction sign to an addition sign, and change the sign of the second number. Then use the integer addition rules.

ex: 
$$-3 - 9 \longrightarrow -3 + (-9) = (-12)$$

ex: 
$$15 - (-8) \longrightarrow 15 + 8 = 23$$

ex: 
$$-6 - (-4) \longrightarrow -6 + 4 = (-2)$$

### Multiplying & Dividing Integers

Ignore the signs and multiply or divide as usual. Then determine the sign of the answer using the following rules:

- Negative · or ÷ Negative = Positive
- Negative · or ÷ Positive (or Positive · or ÷ Negative) = Negative

ex: 
$$-3 \cdot (-5)$$
  $\longrightarrow$   $3 \cdot 5 = 15$   $\longrightarrow$  neg · neg = pos  $\longrightarrow$  answer: (15)

ex: 
$$48 \div (-6)$$
  $\longrightarrow$   $48 \div 6 = 8$   $\longrightarrow$  pos  $\div$  neg = neg  $\longrightarrow$  answer:  $-8$ 

### Order of Operations

Parentheses
Exponents
Multiplication & Division (left to right)
Addition & Subtraction (left to right)

#### Find the sum or difference.

#### Find the product or quotient.

17. 
$$-10 \cdot (-11)$$
 18.  $90 \div (-6)$  19.  $3 \cdot (-59)$  20.  $-7 \cdot (-2)$ 

## Evaluate the numerical expression. (Be sure to use the order of operations!)

# Operations with Rational Numbers

### Adding & Subtracting Rational Numbers

Determine whether you should add or subtract using integer rules. Then add or subtract.

• <u>Decimals</u>: Line up the decimal points. Then add or subtract and bring the decimal point down. Use integer rules to determine the sign of the answer.

ex: -9.8 + 6.24 
$$\longrightarrow$$
 neg + pos: subtract  $\longrightarrow$   $\frac{9.80}{6.24}$   $\longrightarrow$  answer: -3.56

• <u>Fractions/Mixed Numbers</u>: Find a common denominator and then add or subtract. Borrow or convert an improper fraction answer, if necessary. Use integer rules to determine the sign of the answer.

ex: 
$$5\frac{3}{4}$$
- $\left(-3\frac{7}{8}\right)$   $\longrightarrow$   $5\frac{3}{4}$  +  $3\frac{7}{8}$   $\longrightarrow$  pos + pos: add  $\longrightarrow$   $\frac{5\frac{3}{4} = \frac{6}{8}}{8\frac{13}{8}}$   $\longrightarrow$  answer:  $9\frac{5}{8}$ 

### Multiplying & Dividing Rational Numbers

Determine the sign of the answer using integer rules. Then multiply or divide.

<u>Multiplying Decimals</u>: Ignore the decimal points. Multiply the numbers. Then count the
decimal places in the problem to determine the location of the decimal point in the answer.

ex: -9.23 · (-1.1) 
$$\longrightarrow$$
 neg · neg = pos  $\longrightarrow$   $\xrightarrow{\times}$   $\xrightarrow{1.1}$   $\xrightarrow{92.3}$   $\xrightarrow{92.30}$   $\xrightarrow{10.153}$ 

• <u>Dividing Decimals</u>: Move the decimal in the divisor to the end of the number. Move the decimal in the dividend the same number of places and then bring it straight up in quotient.

ex: 
$$-5.2 \div 0.2 \longrightarrow \text{neg} \div \text{pos} = \text{neg} \longrightarrow 02) 52. \longrightarrow \text{answer: } -26$$

<u>Multiplying Fractions</u>: Convert mixed numbers to improper fractions. Then cross-simplify.
 Multiply the numerators and multiply the denominators. Simplify if necessary.

ex: 
$$-1\frac{3}{4} \cdot \frac{6}{14} \rightarrow \text{neg · pos = neg} \rightarrow \frac{17}{2} \cdot \frac{63}{142} = \frac{3}{4} \rightarrow \text{answer: } -\frac{3}{4}$$

 <u>Dividing Fractions</u>: Convert mixed numbers to improper fractions. Then flip the second fraction to its reciprocal and multiply the two fractions. Simplify if necessary.

ex: 
$$-\frac{1}{2} \div \left(-\frac{3}{8}\right) \longrightarrow \text{neg} \div \text{neg} = \text{pos} \longrightarrow \frac{1}{2} \cdot \frac{8}{3} = \frac{4}{3} \longrightarrow \text{answer: } \boxed{\frac{1}{3}}$$

### Find the sum, difference, product, or quotient.

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53. 
$$9 \div (-4^{1}/2)$$
 54.  $-18 + 3^{4}/5$  55.  $-5^{2}/3 \cdot (-2^{5}/6)$  56.  $-5^{3}/4 \cdot (-3^{7}/8)$ 

# Solving Equations

### Solving One-Step Equations

 Cancel out the number on the same side of the equation as the variable by using the inverse operation. (Addition/Subtraction; Multiplication/Division). Be sure to do the same thing to both sides of the equation!

ex: 
$$6x = -18$$
  $\longrightarrow$   $\frac{6x = -18}{6}$   $\longrightarrow$  answer:  $x = -3$ 

ex: 
$$y + 23 = -9$$
  $\longrightarrow$   $y + 23 = -9$   $\longrightarrow$  answer:  $y = -32$ 

ex: 
$$\frac{h}{3} = 4$$
  $\longrightarrow$   $3 \cdot \frac{h}{3} = 4 \cdot 3$   $\longrightarrow$  answer:  $h = 12$ 

ex: 
$$w - 13 = -5$$
  $\longrightarrow$   $w - 13 = -5$   $\longrightarrow$  answer:  $w = 8$ 

# Solving Two-Step Equations

 Undo operations using inverse operations one at a time using the order of operations in reverse. (i.e.: undo addition/subtraction before undoing multiplication/division)

ex: 
$$7x - 4 = -32$$
  $\longrightarrow$   $7x - 4 = -32$   $\longrightarrow$   $7x = -28$   $\longrightarrow$  answer:  $x = -4$ 

ex: 
$$\frac{1}{5}$$
 + 13 = 15  $\longrightarrow$   $\frac{1}{5}$  + 13 = 15  $\longrightarrow$  5 ·  $\frac{1}{5}$  = 2 · 5  $\longrightarrow$  answer:  $1$  = 10

ex: 
$$\frac{b+7}{3} = -2$$
  $\longrightarrow$   $3 \cdot \frac{b+7}{3} = -2 \cdot 3$   $\longrightarrow$   $b+7=-6$   $\longrightarrow$  answer:  $b=-13$ 

### Solve the one-step equation.

57. 
$$19 + j = -34$$

$$58. \text{ m} - 26 = 13$$

59. 
$$\frac{x}{5} = -3$$

60. 
$$12f = 216$$

62. 
$$\frac{h}{9} = 13$$

63. 
$$b + (-3) = -9$$
 64.  $-4w = +280$ 

64. 
$$-4w = +280$$

### Solve the two-step equation.

66. 
$$7 + \frac{y}{2} = -3$$

67. 
$$4 + 3r = -8$$

69. 
$$\frac{k+8}{3} = -2$$

70. 
$$\frac{f}{5}$$
 - (-13) = 12

72. 
$$-8 + 4m = 2$$

$$73.1 - 18 - 13/4 v = 3$$

74. 
$$\frac{-5+n}{4} = -1$$

75. 
$$3.5m + 0.75 = 6.25$$
 76.  $2y + 3 = 19$ 

76. 
$$2y + 3 = 19$$

# Proportions and Percent

## Solving Proportions

• Set cross-products equal to each other and then solve the one-step equation for the given variable.

ex: 
$$\frac{5}{b} = \frac{4}{10}$$
  $\longrightarrow$   $5 \cdot 10 = 4b$   $\longrightarrow$   $\frac{50}{4} = \frac{4b}{4}$   $\longrightarrow$  answer:  $b = 12.5$ 

# Solving Percent Problems with Proportions

• Set up and solve a proportion as follows:  $\frac{4}{100} = \frac{\text{part}}{\text{whole}}$ 

ex: 25 is what percent of 500? 
$$\rightarrow \frac{x}{100} = \frac{25}{500} \rightarrow \text{answer: } x = (5\%)$$

ex: What is 15 \* of 88? 
$$\rightarrow \frac{15}{100} = \frac{x}{88} \rightarrow \text{answer: } x = (13.2)$$

ex: 18 is 30 % of what number? 
$$\longrightarrow \frac{30}{100} = \frac{18}{x} \longrightarrow \text{answer: } x = (60)$$

## Solving Percent Problems with Equations

 Translate the question to an equation and then solve. (Be sure to convert percents to decimals or fractions.)

ex: 20 is 40 % of what number? 
$$\longrightarrow$$
 20 = 0.4x  $\longrightarrow$  answer: x =  $(50)$ 

ex: 8 is what percent of 32? 
$$\longrightarrow$$
 8 = 32x  $\longrightarrow$  x = 0.25  $\longrightarrow$  answer:  $(25*)$ 

ex: What is 25% of 88? 
$$\longrightarrow$$
 x = 0.25 · 88  $\longrightarrow$  answer: x =  $(22)$ 

## Real-World Percent Problems

(This is just one way of many to solve real-world percent problems)

- <u>Tax</u>: Find the amount of tax using a proportion or equation. Then add the tax to the original amount to find the total cost.
- <u>Discount</u>: Find the amount of the discount using a proportion or equation. Then subtract the amount of discount from the original price to find the sale price.

#### Solve the proportion.

77. 
$$\frac{h}{6} = \frac{20}{24}$$

78. 
$$\frac{5}{7} = \frac{c}{14}$$

79. 
$$\frac{6}{8} = \frac{21}{b}$$

80. 
$$\frac{30}{J} = \frac{26}{39}$$

81. 
$$\frac{5}{k} = \frac{15}{20}$$

82. 
$$\frac{32}{112} = \frac{a}{14}$$

83. 
$$\frac{16}{7} = \frac{18}{9}$$

$$84. \ \frac{w}{60} = \frac{15}{200}$$

### Solve the percent problem.

- 85. Find 15% of 85.
- 86. 6 is 75% of what number?
- of 320?
- 87. 40 is what percent 88. What is 20% of 45?

- 89. 70 is what percent 90. Find 33.3% of 81. of 350?
- 91. A \$58 camera is on sale for 20% off. Find the sale price.
- 92. Find the total price of a \$14.00 shirt including the 7% sales tax.

## Geometry

# Geometry Basics

- Perimeter is the distance around a polygon
- Circumference is the distance around a circle
- Area is the space inside a figure
- Volume is the capacity of a 3-dimensional figure
- Surface Area is the sum of the areas of all the faces on a 3-dimensional figure

## 2-Dimensional Geometry Formulas

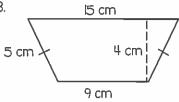
- Perimeter of Any Figure: sum of side lengths
- Circumference =  $\pi$  · diameter
- Area of Parallelogram = base · height
- Area of Triangle =  $\frac{1}{2}$  base · height
- Area of Trapezoid =  $\frac{1}{2}$  · height(base<sub>1</sub> + base<sub>2</sub>)
- Area of Circle = π · radius<sup>2</sup>

# 3-Dimesional Geometry Formulas

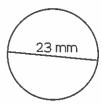
- Volume of Rectangular Prism = length · width · height
- Volume of Cylinder =  $\pi \cdot \text{radius}^2 \cdot \text{height}$
- Surface Area of Rectangular Prism = 2 · length · width + 2 · length · height + 2 · height · width
- Surface Area of Cylinder =  $2 \cdot \pi \cdot \text{radius}^2 + 2 \cdot \pi \cdot \text{radius} \cdot \text{height}$

## Find the perimeter (or circumference) and area. Use 3.14 for pi.

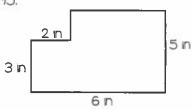
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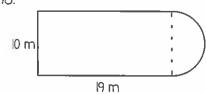
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95.

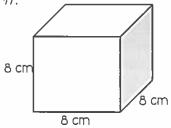


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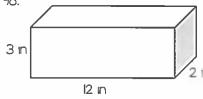


#### Find the surface area and volume.

97.



98.



99.



100.

